



A DIVISION OF ANDREW KALOTAY ASSOCIATES, INC.

Problems with Benchmark Muni Yield Curves

Advanced Curve Building Frameworks: Best Practices



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The Tax-Exempt Bond Market

Large but illiquid (\$3.7 trillion, 60,000 issuers)

Common institutional structure: 5% coupon, par call starting at the end Year 10

Sold well above par; see 'Allure' article in References

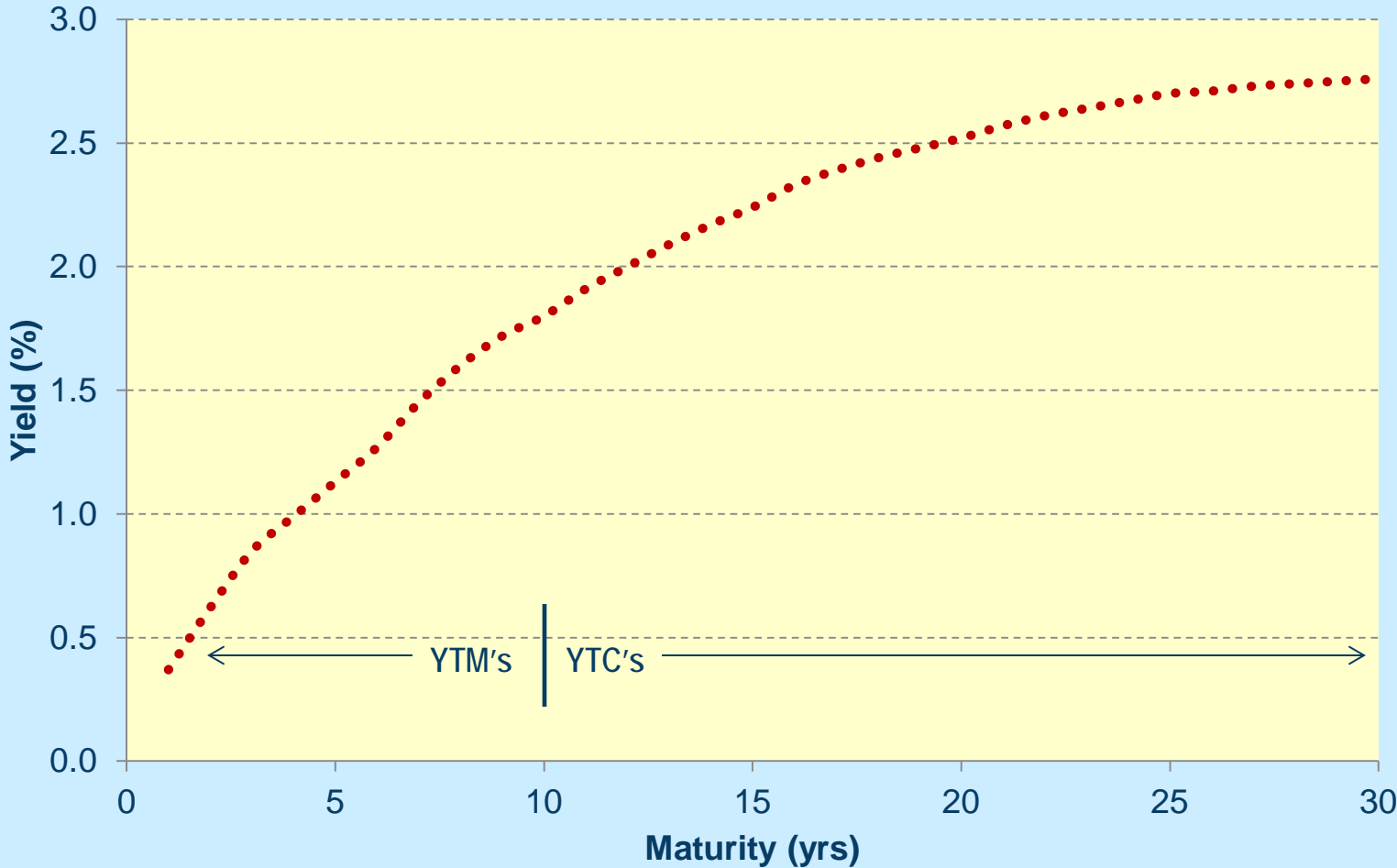
Several vendors provide benchmark 5% NC-10 yield curves (Bloomberg, MMA, MMD, S&P)

Yields are YTC's

Some also provide 5% NCL and par NC-10 curves*

**Different curves by same vendor often inconsistent with each other*

Recent MMA 5% NC-10 Curve



Optionless Discount Rates Needed for Risk Analysis

Have to be inferred from callable benchmark rates

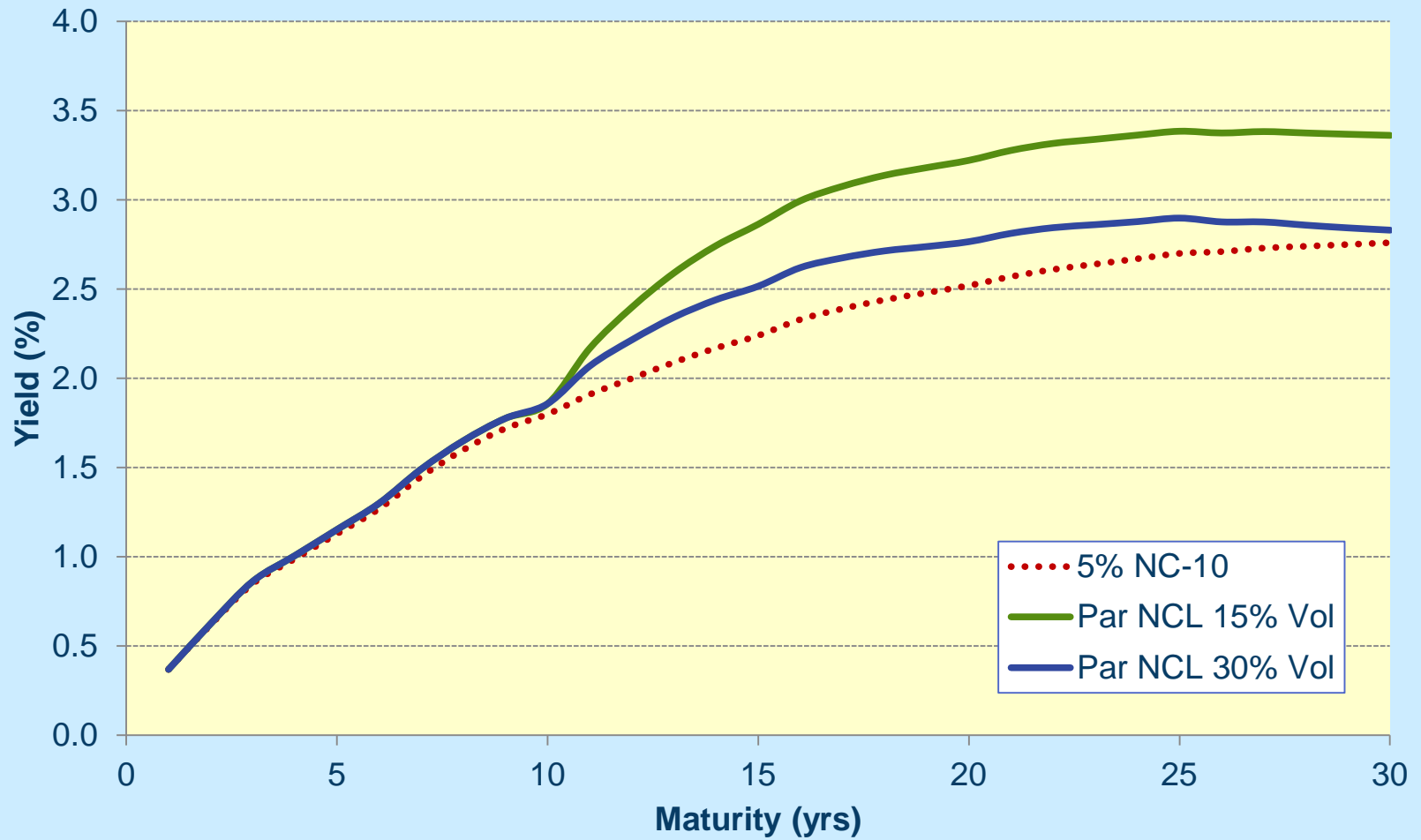
Recommended approach: strip out call options

Specify reasonable interest rate process and volatility

E.g. Black-Karasinski, 15% vol

Bootstrap

Optionless Par Curves



Option Stripping Fails if Curve Not Arbitrage-Free

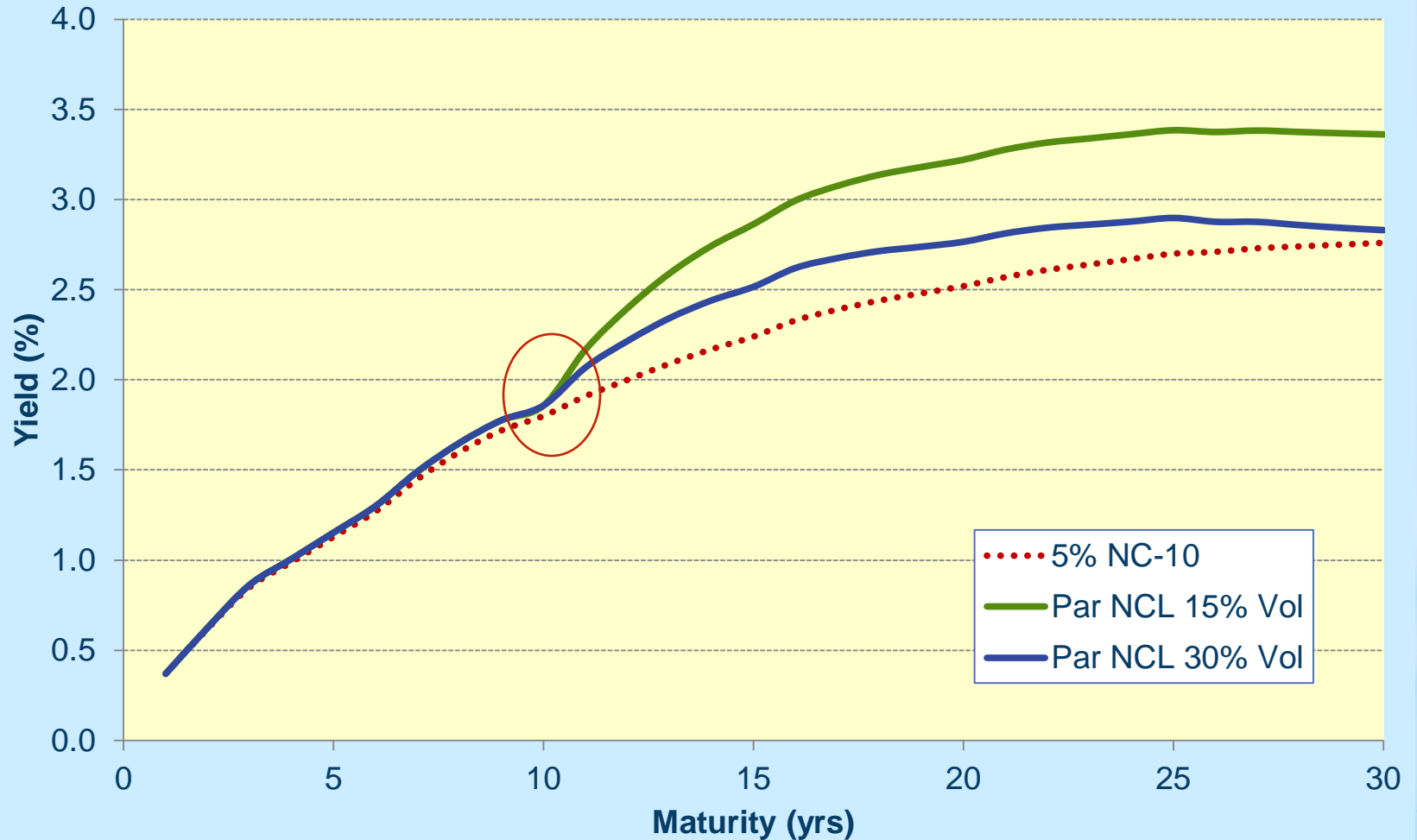
Homework: Prove that

Prices of 5% NC-10 bonds must decline with maturity

Yields of par NC-10 bonds must increase with maturity

See 'Bad curves' in References for proofs

Optionless Curves from Smooth 5% NC-10 Curve



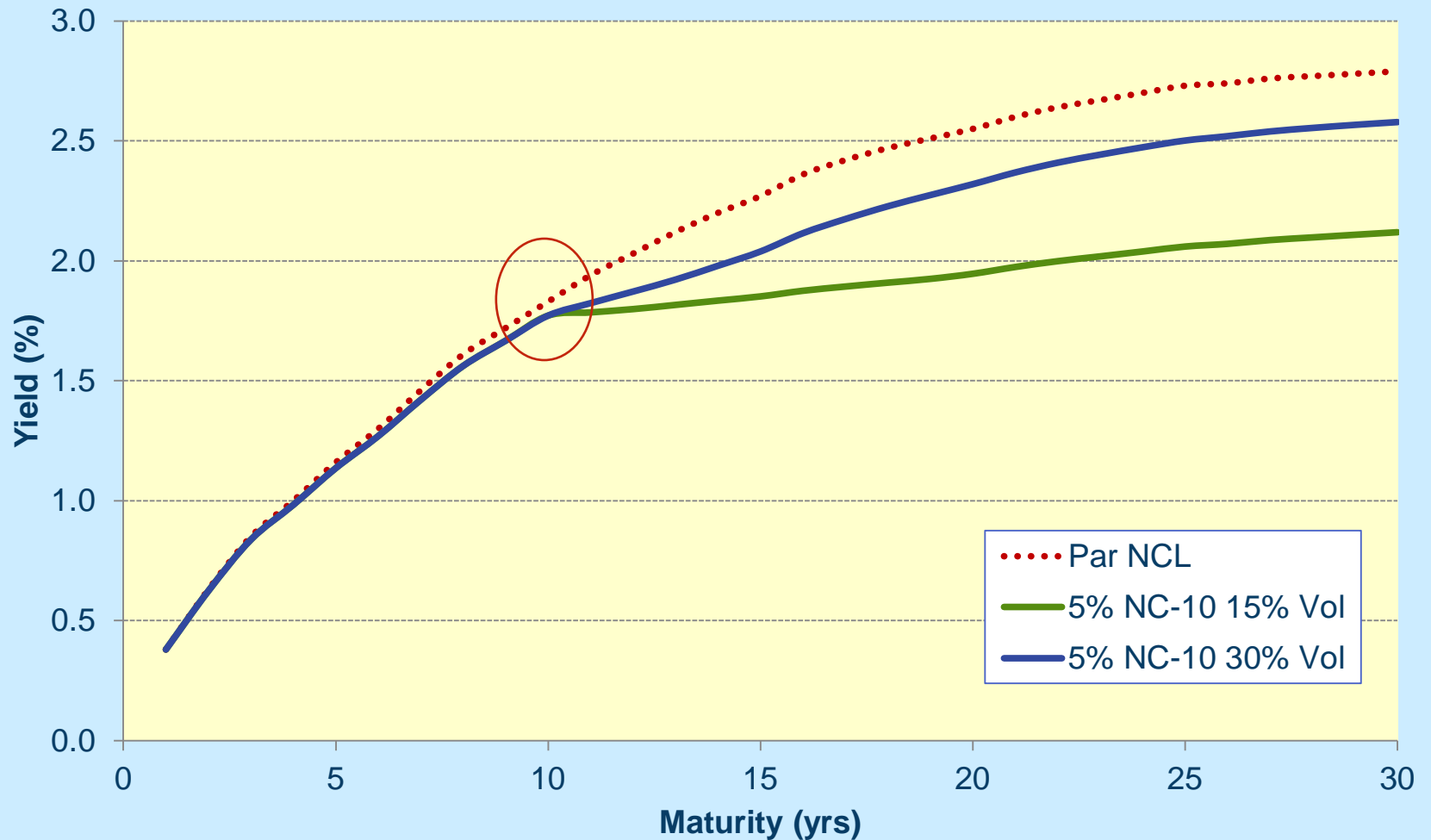
If Callable Curve Is Smooth, NCL Curve Is Not

Bump between Year 10 (optionless) and Year 11 (callable)

Can be reconciled only by using a very high volatility

Similar problem occurs when going from smooth optionless curve to callable curve

5% NC-10 Curves from Smooth NCL Curve



A Career in Munis?

Municipal bonds are rich in optionality, but option-theoretic analytics are sorely missing

Financial engineers looking for a challenge can bring much-needed quantitative rigor to this area

References

What Makes the Municipal Yield Curve Rise? *The Journal of Fixed Income*, Winter 2008

The Interest Rate Sensitivity of Tax-Exempt Bonds under Tax-neutral Valuation, *Journal Of Investment Management*, Vol. 12, No. 1, (2014),

The Allure of 5% Bonds: Coupon Levitation Creates Magical Savings, *The Bond Buyer*, January 27, 2012

Spread(ing) Confusion, *The Bond Buyer*, November 23, 2015

Beware of Bad Benchmark Curves, *The Bond Buyer*, January 6, 2016

Risk(y) Measures, *Forthcoming*